

## Design And Implementation Of 2 Bit Ternary ALU Slice

\*A. P. Dhande \*\*V. T. Ingole

\* Pune Institute Of Computer Technology, Pune, India \*\*College Of Engineering, Badnera, India  
 ashwindhande@pictsctr.edu, vijayingole@hotmail.com

### Abstract

*This paper describes the architecture, design & implementation of 2 bit ternary ALU (T-ALU) slice. The proposed ALU is designed for two-bit operation & can be used for n bit operations by cascading n/2 ALU slices. This ALU is implemented using C-MOS ternary logic gates (T-Gates) for ternary arithmetic & logic circuits. Ternary gates are implemented using enhancement / depletion MOSFET technology, thus proposed ALU is suitable for LSI / VLSI implementation. The designed technique used here requires only two stages i.e. decoder & T-gates, as against three stages i.e. decoder, binary gates & encoder require in conventional ternary logic implementation.*

**Index Terms :** Ternary, Unary function, T-Gates, Literal.

### I. Introduction

Alexander [1964] showed that natural base (e= 2.71828) is the most efficient radix for implementation of switching circuits. It seems that most efficient radix for the implementation of digital system is 3 than 2. Ternary logic system, meaning that it has 3 valued switching. Ternary system has several important advantages over binary. It can be summarized as reductions in the interconnections require to implement logic functions, thereby reducing chip area, more information can be transmitted over a given set of lines, lesser memory requirement for a given data length. Besides this serial & some serial-parallel operations can be carried out at higher speed [1][2][3]. Its advantages have been confirmed in the application like memories, communications and digital signal processing etc. [7].

It has been proven that realization & implementation of combinational & sequential function is possible for ternary systems [4][5][6][7]. The implementation is based around bipolar transistors, MOSFETs etc. a basic switching elements, which is referred to as T-Gates [8].

Besides this several authors have proposed reduction techniques to realize ternary functions [9][10][11][12]. In this contribution, we propose ALU capable of performing basic ternary arithmetic & logic operations as

mentioned in table 1. We also suggest a scheme that takes the advantage of minimization techniques proposed by [9][11][13] & implemented using T-gates designed for ternary operations. This scheme shows reduction in the number of gate count to implement ternary functions. Firstly we describe the design of 2 bit ALU and then integrate over ALU slice.

The organization of paper is: Section II describes basic T-Gate implementation, 2 bit ALU architecture is given in section III, section IV describes 2 bit ALU design and ALU slice design. Experimental results & performance evaluation is given in section V. Finally conclusion is given in section VI.

Table 1:Functional Table of T-ALU

Function select lines		F unctions
W	Z	
0	0	Addition
0	1	Subtraction
0	2	Multiplication
1	0	Compare
1	1	OR
1	2	NOR
2	0	AND
2	1	NAND
2	2	Ex-OR

### II. Ternary logic Gates & Their Implementation

The algebra proposed by Rosenfeld – yoeli [9], which is suitable for arithmetic operations [14] can be realized through ternary logic gates. In this paper three logic levels of T- Gates are represented by states 0,1,2 as  $-V_{cc}$  (-5v), zero potential (0v) &  $+V_{cc}$  (+5v) respectively. The basic ternary inverters namely simple ternary inverter (STI), positive ternary inverter (PTI) & negative ternary inverter (NTI) forms an operator set that is complete in logic sense. All these inverters are combined to realize ternary functions like NAND (T-NAND), NOR (T-NOR) T-AND, T-OR, T-EX-OR etc.

In general ternary inverter, AND & OR functions are defined as:

$$STI = \overline{x^i} = 2 - x$$

$$PTI \ \& \ NTI = \overline{x^i} = i \text{ if } x = i \\ = 2 - i \text{ if } x \neq i \text{ where } i \text{ can be } 2 \text{ or } 0$$

$$TOR = \text{Max} (x, y) \ \& \ TAND = \text{Min} (x, y)$$

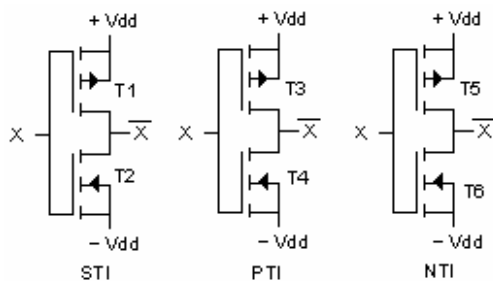
Fig.1 (a) shows implementation of basic ternary inverters, (b) truth table & (c) symbols for inverters respectively. Table 2 gives threshold values  $v_T$  requires to implement ternary inverters. Depending upon inverters used, positive ternary NAND (PTNAND), negative ternary AND (NTAND) etc. functions can realize. We have implemented T-Gates using P & N channel enhancement / depletion MOSFETs. Figure 2 (a) shows T-NAND, T-NOR implementation, (b) symbols & (c) truth table.

- (b) Truth table for ternary inverters.
- (c) Symbols for T-Gates.

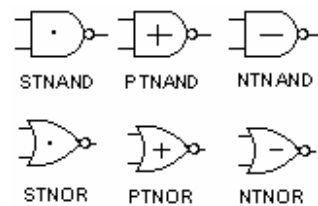
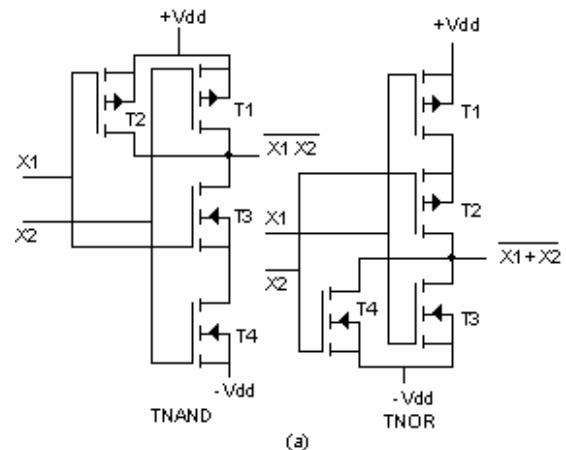
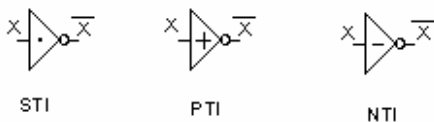
For the implementation of standard ternary inverters  $1M\Omega$  resistances are actually connected between the drains of MOSFETS.

Table 2. Threshold values for inverters

Inverters	Transistor	Device type	$V_{th}$	Device	Drain ohmic resistance
STI	T1	p channel enhancement	-0.45v	international IRFD 9110	$1M\Omega$
	T2	n channel enhancement	0 v	international IRF 360	$1M\Omega$
PTI	T3	p channel enhancement	-0.25	International IRF 9640	$0.44143 \Omega$
	T4	n channel enhancement	4.137	Harris IRF222	$0.67 \Omega$
NTI	T5	p channel enhancement	2.69 v	Harris IRF 220	$0.36731\Omega$
	T6	n channel enhancement	-5v	Fairchild FQ99p25	$0.62\Omega$



Input X	STI	PTI	NTI
0	2	2	2
1	1	2	0
2	0	0	0



X1 X2	STAND	STOR	STNAND	NTNAND	STNOR	NTNOR
0 0	0	0	2	2	2	2
0 1	0	1	2	2	1	0
0 2	0	2	2	2	0	0
1 0	0	1	2	2	1	0
1 1	1	1	1	0	1	0
1 2	1	2	1	0	0	0
2 0	0	2	2	2	0	0
2 1	1	2	1	0	0	0
2 2	2	2	0	0	0	0

Fig.1 (a) Implementation of T-Gates.

Fig.2. (a) T-NAND T-NOR Implementation  
(b) Symbols (c) Truth table

### III. T-ALU Architecture & Working

Block diagram & architecture of proposed T-ALU is shown in fig.3 (a) and 3(b). Its functions are given in table 1. The operating voltages required are +5 & -5v. Main building blocks of ALU are function selection logic, C-MOS transmission gates & separate processing modules like adder, subtractor, comparator etc.

Function selection lines W & Z activates respective module by enabling C-MOS transmission gate (TG), while other modules are deactivated from data lines (decoder output lines). Output equation of function block is  $Y = w^0 z^0 + w^0 z^1 + w^0 z^2 + w^1 z^0 + w^1 z^1 + w^1 z^2 + w^2 z^0 + w^2 z^1 + w^2 z^2$ . When function selection lines are activated by ternary I/P, O/P of selection logic is high i.e.2 for corresponding I/P. This high O/P enable TG associated with respective module which connects data lines to the module while other modules are isolated from data lines. When TG [15] enable signal is low i.e.0, TG is opened (high impedance state =1v). Thus any function listed in table 1 can be realized.

Decoder in the circuit generates unary functions for input variable x as  $x^0, x^1$  &  $x^2$  which is used for ternary function implementation. Table 4 is unary function table for I/P x. Fig.4 gives implementation of decoder by T-Gates. In fig.5 (a) implementation of TG & (b) symbol is given. Fig.6 describe implementation of ternary function with the designed technique used in this paper & Fig.7 shows connectivity of single module with TG & decoder.

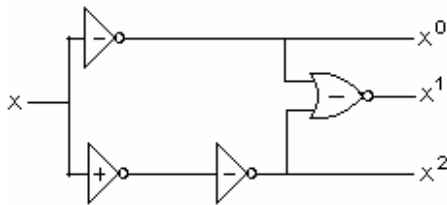


Fig.4. Implementation of decoder

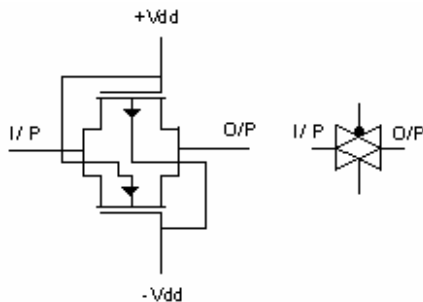


Fig.5. (a) Implementation of TG  
(b) Symbol for TG

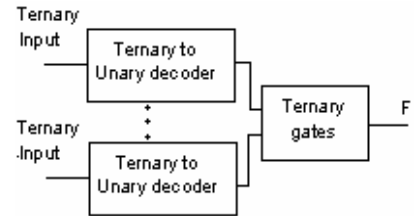


Fig.6. Implementation of ternary function.

Table.4 Unary function table

x	$x^0$	$x^1$	$x^2$
0	2	0	0
1	0	2	0
2	0	0	2

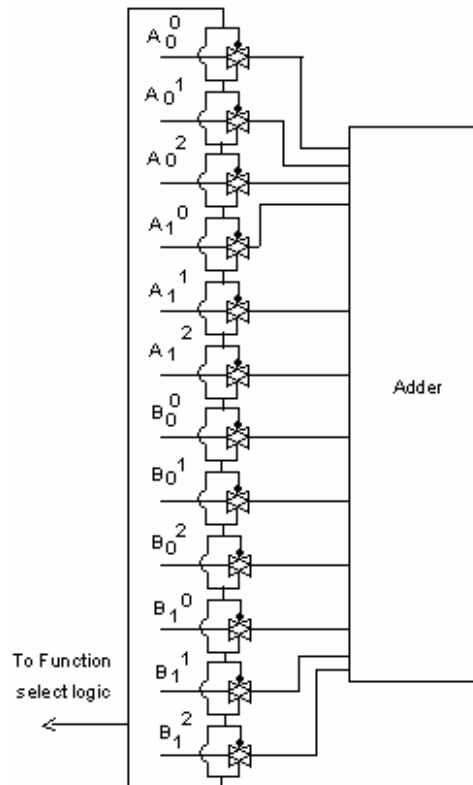


Fig.7. Connectivity of TG with module

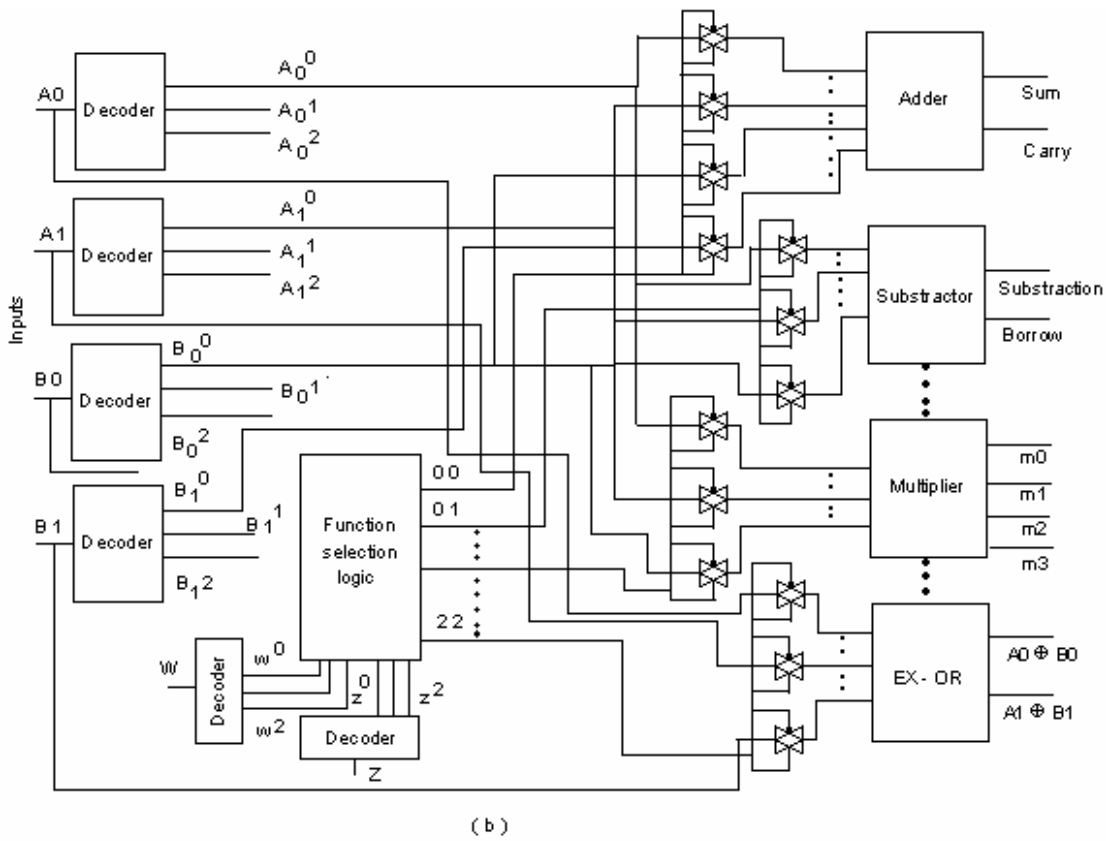
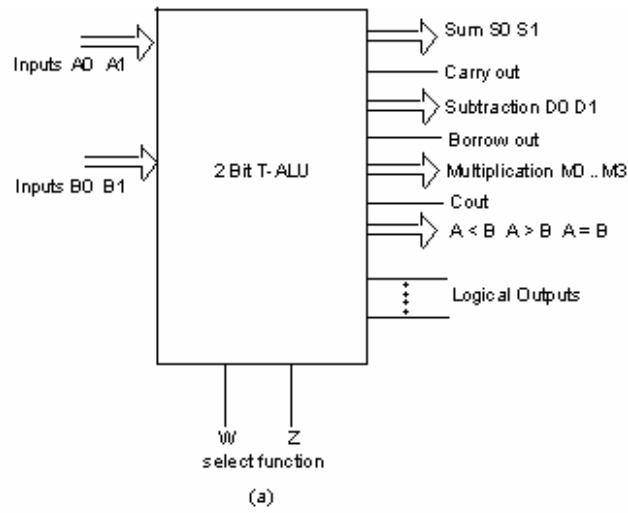


Fig.3. (a) Block diagram of T-ALU  
(b) Architecture of T-ALU

### IV. T-ALU Design

Design of ALU is based on ternary K-map method for ternary function minimization [9], out of various methods suggested in ref. [10] [11] [12] [13]. Here we describe the design of adder, multiplier Ex-OR & comparator modules. Same design concept is implemented for designing other modules.

#### IV (A). Design of Adder module

Design rules for ternary addition is given in the table-5. For two-bit addition of ternary numbers one full & one half-ternary adder is required. Truth table for half & full adder is given in appendix I. Fig.8 (a) shows block diagram of adder module (b) ternary kmap for half adder & (c) ternary k-map for full adder. Fig.9 shows T-gate implementation of half adder. The output equations for half adder are  $Sum = A_0^2 B_0^0 + A_0^1 B_0^1 + A_0^0 B_0^2 + 1$ .  $(A_0^1 B_0^0 + A_0^0 B_0^1 + A_0^2 B_0^2)$

Carry =  $1 \cdot (A_0^2 B_0^1 + A_0^1 B_0^2 + A_0^0 B_0^0)$  Similarly, output equations for full adder is

$$Sum = C_{in}^0 [A_1^2 B_1^0 + A_1^1 B_1^1 + A_1^0 B_1^2] + C_{in}^1 [A_1^1 B_1^0 + A_1^0 B_1^1 + A_1^2 B_1^2] + C_{in}^2 [A_1^0 B_1^0 + A_1^2 B_1^1 + A_1^1 B_1^2] + 1 \cdot \{ [C_{in}^0 (A_1^1 B_1^0 + A_1^0 B_1^1 + A_1^2 B_1^2)] + [C_{in}^1 (A_1^0 B_1^0 + A_1^2 B_1^1 + A_1^1 B_1^2)] + [C_{in}^2 (A_1^2 B_1^0 + A_1^1 B_1^1 + A_1^0 B_1^2)] \}$$

$$Carry = A_1^2 B_1^2 C_{in}^2 + 1 \cdot [A_1^2 B_1^1 C_{in}^0 + A_1^2 B_1^0 C_{in}^1 + A_1^1 B_1^2 C_{in}^0 + A_1^1 B_1^1 C_{in}^1] + 2 [(B_1^1 C_{in}^2 + B_1^2 C_{in}^2) + (B_1^2 C_{in}^2 + B_1^1 C_{in}^1) + (A_1^1 C_{in}^2 + A_1^2 C_{in}^1) + (A_1^2 C_{in}^1 + A_1^1 C_{in}^0)]$$

Table 5. Design rules for ternary addition

A	B	Sum	Carry
0	0	0	0
0	1	1	0
0	2	2	0
1	1	2	0
1	2	0	1
2	2	1	1

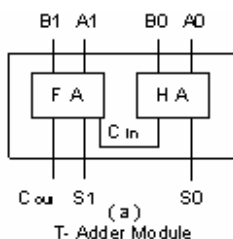


Fig.8 (a) Adder module, (b) K-map for half adder (c) K-map for full adder

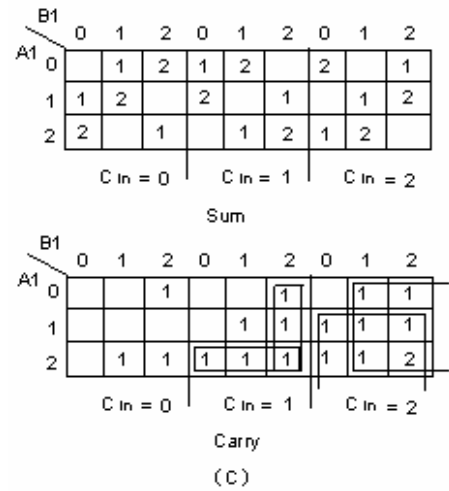
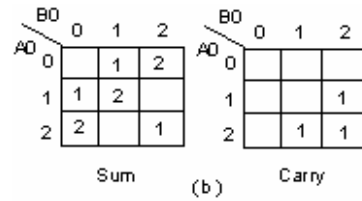
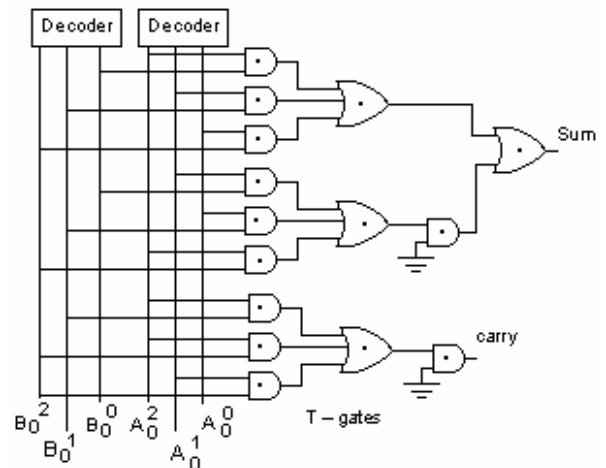


Fig.9. Implementation of half adder



**IV (B). Design of Multiplier module**

Multiplication of n-bit ternary number requires generation of partial product, shifting operations & finally addition of partial product. We have implemented multiplier block as a combination of 1-bit ternary multiplier, half and full T adders. Table 6 (a) shows rules for multiplication, (b) truth table for 1-bit multiplier along with KMap for 1-bit multiplier. Fig.10 Shows implemented ternary multiplier blocks. The output equation of 1 bit multiplier is  $F_{mul} = A_0^2 B_0^1 + B_0^2 A_0^1 + 1 \cdot (A_0^1 B_0^1 + A_0^2 B_0^2)$ .

$F_{carry} = 1 \cdot (A_0^2 + B_0^2)$

Table-6 (a) Rules for multiplication  
(b) Truth table for 1-bit multiplication

A	B	Product	Carry
0	0	0	0
0	1	1	0
0	2	2	0
1	1	1	0
1	2	0	1
2	2	1	1

A	B	Product	Carry
0	0	0	0
0	1	0	0
0	2	0	0
1	0	0	0
1	1	1	0
1	2	2	0
2	0	0	0
2	1	2	0
2	2	1	1

(a) (b)

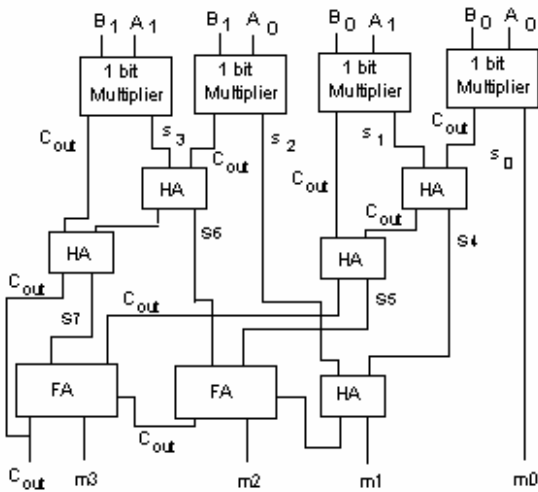
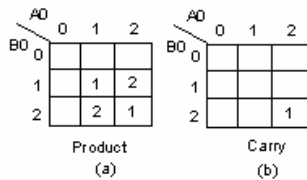


Fig.10 1bit ternary multiplier

**IV (C). Design of comparator module**

Block diagram for 2bit comparator is shown in fig.11. Appendix II gives truth table for comparator. Ternary k-map for condition A=B, A>B & A<B where A= A0,A1 & B= B0,B1 is shown below. From k-map output equations are

$A=B = (A_1^0 B_1^0 + A_1^1 B_1^1 + A_1^2 B_1^2) [A_0^0 B_0^0 + A_0^2 B_0^2] + A_0^1 B_0^1 [A_1^0 B_1^0 + A_1^1 B_1^1 + A_1^2 B_1^2]$ .

$A < B = A_0^0 A_1^1 B_0^1 B_1^1 + A_0^0 A_1^2 B_0^2 B_1^1 + A_0^0 A_1^1 B_0^2 B_1^1 + A_0^1 A_1^1 B_0^2 B_1^1 + 2A_0^1 B_1^1 + 2A_0^0 B_1^2 + 2A_1^1 B_1^2 + 2B_0^2 B_1^1 [A_0^0 + A_0^1] + A_0^0 A_1^1 B_0^1 + 2A_1^0 B_0^2 [A_0^0 + A_0^1]$

$A > B = A_0^2 A_1^1 B_0^0 B_1^1 + A_0^1 A_1^1 B_0^0 B_1^1 + A_0^2 A_1^1 B_0^1 B_1^1 + A_0^2 A_1^2 B_0^1 B_1^1 + A_0^2 A_1^2 B_0^2 B_1^1 + 2B_0^0 B_1^1 [A_0^1 + A_0^2] + 2A_1^2 B_1^0 + 2A_1^1 B_1^0 + 2A_1^2 B_1^0$

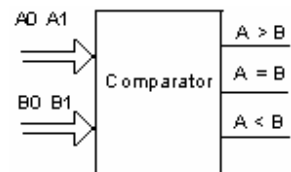
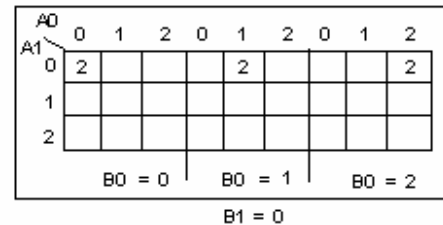
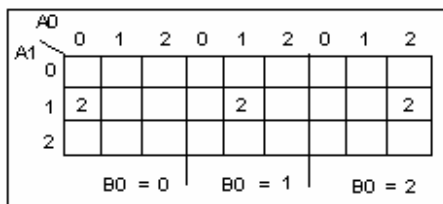


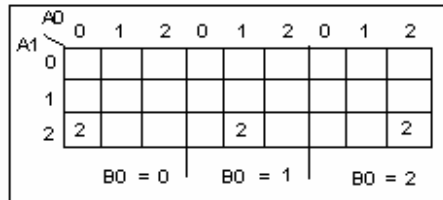
Fig.11. Comparator block



B1 = 0

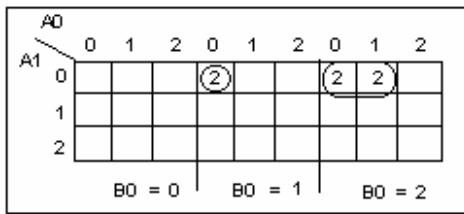


B1 = 1

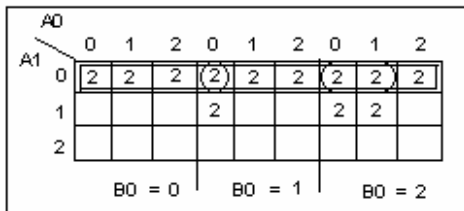


B1 = 2

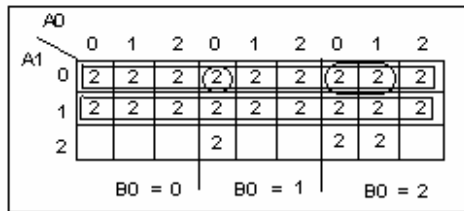
(a) k-map for A = B



B1 = 0



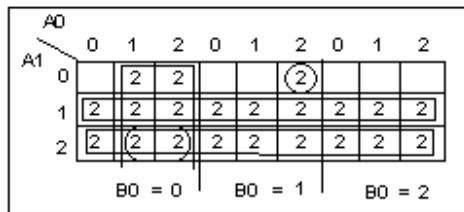
B1 = 1



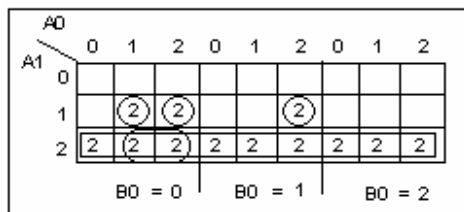
B1 = 2

(b)

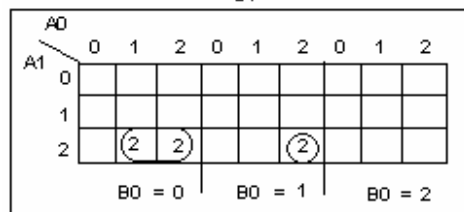
k-map for  $A < B$



B1 = 0



B1 = 1



B1 = 2

(c)

k-map for  $A > B$

### IV (d). Design of Ex-OR module

Ternary Ex-OR function is mod-3 addition of ternary numbers & neglecting carry generated [16]. Ex-OR function is implemented using half adders. Fig.12 is block for Ex-OR module. Rules for mod-3 addition is given in table 7 (a) & (b) is truth table for Ex-Oring of 2-bit number.

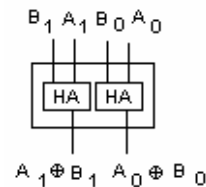


Fig. 12 Block for Ex-OR Module

Table 7 (a) Rules for Ex-OR operation  
(b) Truth table for 2-bit Ex-OR

A	0	1	2
B <sub>0</sub>	0	1	2
1	1	2	0
2	2	0	1

(a)

B <sub>1</sub>	B <sub>0</sub>	A <sub>1</sub>	A <sub>0</sub>	A <sub>0</sub> ⊕ B <sub>0</sub>	A <sub>1</sub> ⊕ B <sub>1</sub>
0	0	0	0	0	0
0	0	0	1	1	0
...	...	...	...	...	...
2	2	2	2	1	1

(b)

### IV B. Implementation Of 2-Bit slice

The proposed design of 2-bit ALU is extended for implementing ALU slice. Block diagram of slice is shown in fig-13. Cascading inputs carry, borrow has to be connected carry, borrow,  $A=B, A>B, A<B$  to of next slice for n-bit slice else connect carry, borrow to ground &  $A=B, A>B, A<B$  to Vcc. Modifications required for ALU slice in 2bit ALU is shown in fig.14(a) (b)& (c). For Comparator, the output of present stage is connected to terminal 1, and previous stage output is connected to terminal 2 of circuit as in fig (c). For implementing n-bit logic functions no modification is required. For example to implement 4 bit logical AND operation, 2 slices are required out of which A0 A1 B0 B1 is to be connected slice 1 & A2 A3 B2 B3 is to be connected slice 2.

As the number of bits increases, multiplication becomes more complex. We have used the multiplier block as described in ref [3].

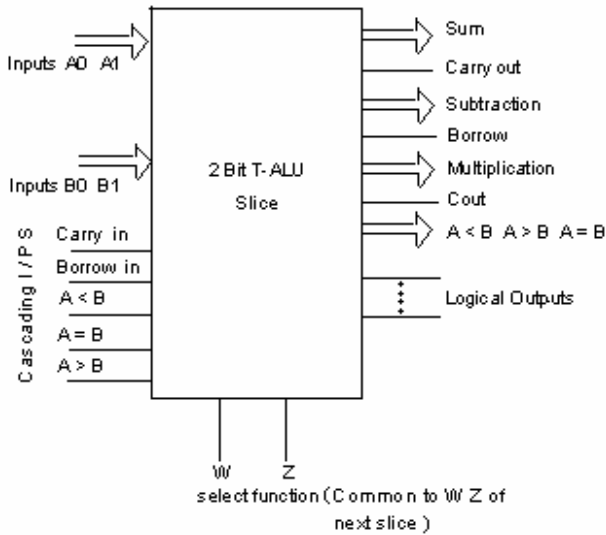


Fig.13 T-ALU Slice

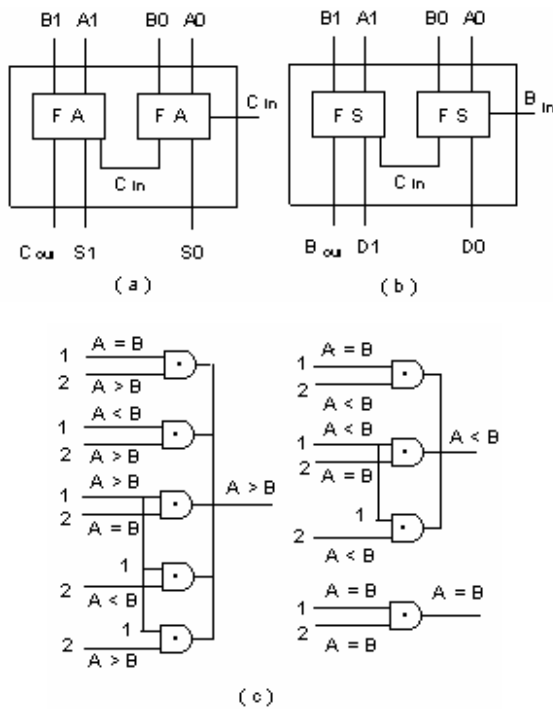


Fig.14 Modifications for ALU slice

### V. Experimental verification & performance evolution

Experimental circuits are designed & implemented to verify workings of some modules of proposed ALU. These circuits are build using logic gates specified in section II. Typical experimental results are presented for adder, multiplier, & Ex-OR operations & as seen desired operations are achieved. Fig15(a) shows storage oscilloscope waveform for adder module when B1=1 B0=2, A1=0, A0=2. , ( b ) is output of multiplier module when B1=2, B0=2, A1=2, A0=2 & finally ( C ) shows Ex-OR operation B1= 1, B0=0 ,A1=1, A0=0.

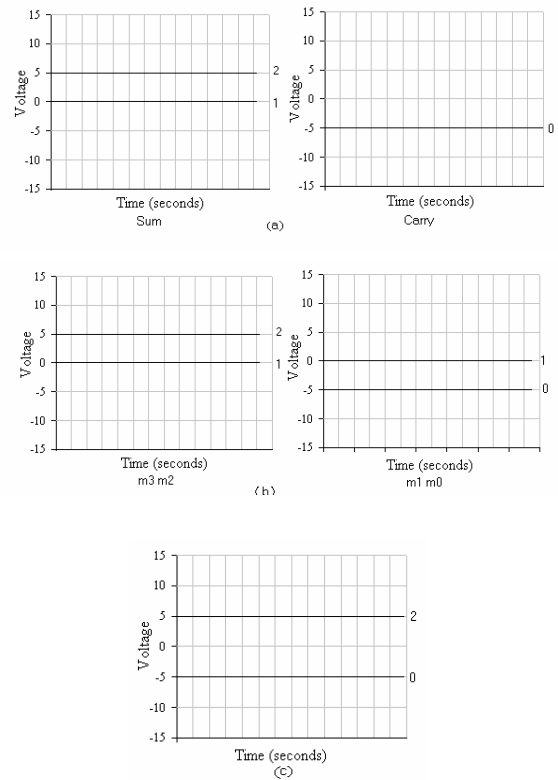


Fig.15 (a) DSO waveforms for Adder module. (b) Multiplier output (C) Ex-OR output

### Performance evaluation

We make the performance evolution on the basis of implementation of ternary logic function in comparison with scheme proposed in [3] [5] [10] [13] with respect to hardware complexity. Here we compare number of gates



required for the implementation of half / full adders / subtractor. A half adder of type [3][5][10][13] requires 13,20,17,30 binary gates respectively & encoder as an additional block for binary to ternary encoding where as in proposed scheme 15 T-gates are required without encoder. Same analogy can be extended for full adder. Here with the proposed scheme number of T-gates required are 56 compared to 108,115,83 & 120 binary gates for references [3][5][10][13].

Furthermore our T-gates have significant reduction in power dissipation, deduced propagation delay etc as compared with [3][5][10]. Table 8 gives average propagation delay comparison with T-gates proposed in [3]. These results are obtained by simulating the circuits on P-Spice simulation program.

Table 8: Propagation-delay comparison

	scheme based on T-Gates	scheme based on binary gates *
	Ave. propagation delay	Ave. propagation delay
Half adder	6 $\tau$	7 $\tau$
Full adder	7 $\tau$	8 $\tau$
Full subtractor	6 $\tau$	—

\* Ref [3]

$\tau$  = Ave. propagation delay of 1 MOSFET

## VI. Conclusion

A complete architecture, design & implementation of 2-bit ALU slice is describe. The scheme based on improved ternary logic gate is also described. It exhibits significant advantages of reduction in circuit complexity, low static power consumption & increased speed of operation.

The ALU can be extended to implement more function with modification in selection logic, decoder etc. Thus it can be incorporated as processing unit for ternary microprocessors.

The ternary logic functions can also be implemented using ternary PLAs [17] thereby increasing packing density, more complex function implementation etc. for future advancement.

## VIII. References

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**Appendix-I**

Truth-Table For Half & Full Adders

Half Adder				Full Adder				
X2	X1	Sum	Carry	X2	X1	C in	Sum	Carry
0	0	0	0	0	0	0	0	0
0	1	1	0	0	0	1	1	0
0	2	2	0	0	0	2	2	0
1	0	1	0	0	1	0	1	0
1	1	2	0	0	1	1	2	0
1	2	0	1	0	1	2	0	1
2	0	2	0	0	2	0	2	0
2	1	0	1	0	2	1	0	1
2	2	1	1	0	2	2	1	1
1	0	0	0	1	0	0	1	0
1	0	1	2	1	0	1	2	0
1	0	2	0	1	0	2	0	0
1	1	0	2	1	1	0	2	0
1	1	1	0	1	1	1	0	1
1	1	2	1	1	1	2	1	1
1	2	0	0	1	2	0	0	1
1	2	1	1	1	2	1	1	1
1	2	2	2	1	2	2	2	1
2	0	0	2	2	0	0	2	0
2	0	1	0	2	0	1	0	1
2	0	2	1	2	0	2	1	1
2	1	0	0	2	1	0	0	1
2	1	1	1	2	1	1	1	1
2	1	2	2	2	1	2	2	1
2	2	0	0	2	2	0	0	1
2	2	1	1	2	2	1	1	1
2	2	2	2	2	2	2	2	2

The design procedure is

- 1) Construct truth table & k-map for input variable.
- 2) Find the cell grouping if possible. i.e. grouping of 1 x 3, 2 x 3, 3 x 3 of 2's term and 1's terms if possible. For grouping of 1's, 2 can be considered as don't care terms.
- 3) Deduce, minimize & realize the switching function.
- 4) The minimization equation is  $F = f1 + 1.f2$

**Appendix II**

Truth tables for comparators & Multiplier

Multiplier Truth Table

B1	B0	A1	A0	m <sub>3</sub>	m <sub>2</sub>	m <sub>1</sub>	m <sub>0</sub>
0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	0
0	0	1	2	0	0	0	0
0	1	1	0	0	0	0	0
0	1	2	1	0	0	0	1
0	1	2	2	0	0	0	2
0	2	0	0	0	0	0	0
0	2	1	1	0	0	0	2
0	2	2	2	0	0	1	2
⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮
1	0	0	0	0	0	0	0
1	0	0	1	0	0	0	1
1	0	1	2	0	1	2	0
1	1	1	0	0	0	1	0
1	1	2	1	1	1	0	1
1	1	2	2	2	1	0	2
1	2	0	0	0	0	0	0
1	2	1	1	0	0	0	2
1	2	2	2	2	1	1	2
⋮	⋮	⋮	⋮	⋮	⋮	⋮	⋮
2	0	0	0	0	0	0	0
2	0	0	1	0	0	2	0
2	0	1	2	1	0	1	0
2	1	1	0	0	2	1	0
2	1	2	1	1	2	1	1
2	1	2	2	2	0	0	2
2	2	0	0	0	0	0	0
2	2	1	1	1	1	1	2
2	2	2	2	2	1	0	1

Comparator Truth Table

B1	B0	A1	A0	A < B	A = B	A > B
0	0	0	0	0	2	0
0	0	0	1	0	0	2
0	0	1	2	0	0	2
0	1	1	0	0	0	2
0	1	2	1	0	0	2
0	1	2	2	0	0	2
0	2	0	0	2	0	2
0	2	1	1	0	0	2
0	2	2	2	0	0	2
⋮	⋮	⋮	⋮	⋮	⋮	⋮
1	0	0	0	2	0	0
1	0	0	1	2	0	2
1	0	1	2	2	0	2
1	1	1	0	2	0	0
1	1	2	1	0	0	2
1	1	2	2	0	0	2
1	2	0	0	2	0	0
1	2	1	1	2	0	0
1	2	2	2	0	0	2
⋮	⋮	⋮	⋮	⋮	⋮	⋮
2	0	0	0	2	0	0
2	0	0	1	2	0	0
2	0	1	2	2	0	0
2	1	1	0	2	0	0
2	1	2	1	0	2	0
2	1	2	2	0	0	2
2	2	0	0	2	0	0
2	2	1	1	2	0	0
2	2	2	2	0	2	0